

Lesson 1-8 – Multiplying Big Integers

Objectives:

- Students will multiply multi-digit integers, as evidenced by their completion of ALEKS skills where they do so.
- Students will memorize the multiplication table, as evidenced by them passing “minute quizzes.”

Student Materials on Desk Corner:

- Multiplying Integers Homework
- Homework Checker
- Readiness Checker

Student Materials for Later:

- Homework Log
- Binder Paper
- Pencils

Teacher Materials:

- “Minute Quiz 8A”
- “Multiplying Integers Homework” answer key and grading roster for TA
- “Multiplying Integers Homework #2” handout

Homework:

- Multiplying Integers Homework #2
- Study for Minute Quiz

Time	Activity
Before Bell	<p style="text-align: center;">DO NOW</p> <p>As students enter the classroom, shake hands and remind them that there is a minute quiz and they need to be seated quietly with a pencil when the bell rings.</p> <p>Write the following “Do Now” on the board:</p> <ul style="list-style-type: none"> • Take out a pencil and <i>quietly</i> wait for the minute quiz.
5 min	<p style="text-align: center;">MINUTE QUIZ</p> <p>When the bell rings, quickly go around and put the minute quiz on each student’s desk, facedown. Then, start the quiz and give everyone one minute.</p> <p>While students are working on the quiz, quickly stamp the readiness checkers of students who are ready when the bell rings and have their readiness checkers out.</p>
30 min	<p style="text-align: center;">ALEKS</p> <p>Students should continue with ALEKS. While they work, have the TA go around and collect homework and stamp homework checkers. Take attendance and return graded homework.</p>
1 min	<p style="text-align: center;">STRETCH BREAK</p> <p>Before transitioning to the lecture, lead the students through some exercises to refresh them.</p>
44 min	<p style="text-align: center;">LESSON: MULTIPLYING BIG INTEGERS</p> <p>Notes Follow the handwritten Cornell Notes.</p> <p>Homework Pass out the “Multiplying Integers Homework #2” handout and have students write down the assignment on their homework logs. Also remind students that there will be a minute quiz again the next time we meet on the new homework assignment (multiplying 4’s, 5’s, and 6’s).</p>

Solve the following multiplication problems. You have exactly one minute!

$7 \cdot 1 =$	$3 \cdot 1 =$	$8 \cdot 2 =$
$10 \cdot 2 =$	$12 \cdot 2 =$	$9 \cdot 1 =$
$9 \cdot 3 =$	$8 \cdot 2 =$	$9 \cdot 1 =$
$8 \cdot 1 =$	$2 \cdot 1 =$	$5 \cdot 1 =$

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$9 \cdot 3 =$	$8 \cdot 2 =$	$9 \cdot 1 =$
$8 \cdot 1 =$	$2 \cdot 1 =$	$5 \cdot 1 =$

Solve the following multiplication problems. You have exactly one minute!

$4 \cdot 2 =$

$3 \cdot 3 =$

$8 \cdot 3 =$

$6 \cdot 1 =$

$8 \cdot 1 =$

$9 \cdot 2 =$

$8 \cdot 3 =$

$12 \cdot 1 =$

$2 \cdot 2 =$

$5 \cdot 2 =$

$11 \cdot 2 =$

$12 \cdot 1 =$

Solve the following multiplication problems. You have exactly one minute!

$4 \cdot 2 =$

$3 \cdot 3 =$

$8 \cdot 3 =$

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$8 \cdot 1 =$

$9 \cdot 2 =$

$8 \cdot 3 =$

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$3 \cdot 3 =$

$8 \cdot 3 =$

$6 \cdot 1 =$

$8 \cdot 1 =$

$9 \cdot 2 =$

$8 \cdot 3 =$

$12 \cdot 1 =$

$2 \cdot 2 =$

$5 \cdot 2 =$

$11 \cdot 2 =$

$12 \cdot 1 =$

Solve the following multiplication problems. You have exactly one minute!

$3 \cdot 2 =$

$10 \cdot 1 =$

$9 \cdot 2 =$

$2 \cdot 1 =$

$7 \cdot 2 =$

$5 \cdot 2 =$

$2 \cdot 2 =$

$11 \cdot 2 =$

$9 \cdot 2 =$

$9 \cdot 2 =$

$2 \cdot 1 =$

$12 \cdot 1 =$

Solve the following multiplication problems. You have exactly one minute!

$3 \cdot 2 =$

$10 \cdot 1 =$

$9 \cdot 2 =$

$2 \cdot 1 =$

$7 \cdot 2 =$

$5 \cdot 2 =$

$2 \cdot 2 =$

$11 \cdot 2 =$

$9 \cdot 2 =$

$9 \cdot 2 =$

$2 \cdot 1 =$

$12 \cdot 1 =$

Solve the following multiplication problems. You have exactly one minute!

$3 \cdot 2 =$

$10 \cdot 1 =$

$9 \cdot 2 =$

$2 \cdot 1 =$

$7 \cdot 2 =$

$5 \cdot 2 =$

$2 \cdot 2 =$

$11 \cdot 2 =$

$9 \cdot 2 =$

$9 \cdot 2 =$

$2 \cdot 1 =$

$12 \cdot 1 =$

Multiplying Big Integers, Part 1

Section → Intro

We multiply small integers by adding (ex: $2 \cdot 3 = 2 + 2 + 2 = 6$)
by
or memorizing the mult table.

We usually mult big ints like:

For big integers, we usually use long mult'n ^{following} the ~~method~~.

Ex:
$$\begin{array}{r} 123 \\ \times 8 \\ \hline 984 \end{array}$$

This has 2 problems:

- 1) must remember to carry
- 2) hard to see why it works

Instead, we will learn the method of partial products
(also known as long mult'n).

Section → Distributive Property (D.P.)

★ The D.P. lets us multiply across parenthesis.

Ex: $2(3+4) = 2 \cdot 3 + 2 \cdot 4$

Let's show it's true.

Left: $2(3+4) = 2 \cdot 7 = 14$

Right: $2 \cdot 3 + 2 \cdot 4 = 6 + 8 = 14$

Ex: $2(3+4+5) = 2 \cdot 3 + 2 \cdot 4 + 2 \cdot 5$

$$\text{Ex: } (7+8) \cdot 9 = 7 \cdot 9 + 8 \cdot 9$$

Section → Partial Product Mult

Idea: ~~we break apart the number~~ ^{We} multiply ~~the smaller pieces~~ ^{the smaller pieces}, ~~multiply them separately~~ ^{multiply them separately}, and then add them ~~back~~ together.

Ex: $123 \cdot 8 = ?$

Why this works: ~~break apart 123 = 100 + 20 + 3~~
 then $123 \cdot 8 = (100 + 20 + 3) \cdot 8$

$$= 100 \cdot 8 + 20 \cdot 8 + 3 \cdot 8$$

↑ ↑ ↑
 these are much easier pieces

$$= 800 + 160 + 24 \quad \text{add the results together}$$

$$= 984$$

$$\begin{array}{r} 123 \\ \times 8 \\ \hline 24 \leftarrow 8 \cdot 3 \\ 160 \leftarrow 8 \cdot 20 \\ + 800 \leftarrow 8 \cdot 100 \\ \hline 984 \end{array}$$

Ex: $123 \cdot 9 = ?$

$$\begin{array}{r} 123 \\ \times 9 \\ \hline 27 \leftarrow (3 \cdot 9) \\ 180 \leftarrow (20 \cdot 9) \\ + 900 \leftarrow (100 \cdot 9) \\ \hline 1107 \end{array}$$

Ex: $7248 \cdot 3 = ?$

~~$$\begin{array}{r} 7248 \\ \times 3 \\ \hline 24 \\ 120 \\ 600 \\ + 2100 \\ \hline 2884 \end{array}$$~~

$$\begin{array}{r} 7,248 \\ \times 3 \\ \hline 24 \leftarrow 8 \cdot 3 \\ 120 \leftarrow 40 \cdot 3 \\ 600 \leftarrow 200 \cdot 3 \\ + 21,000 \leftarrow 7000 \cdot 3 \\ \hline 21,744 \end{array}$$

